

# Progress Report

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Current work is aimed at studying the effect of strain rate on the void growth and to formulate a closed form solution for yield function for the porous material. The closed form yield function for spherical and cylindrical voids shapes are already derived in Gurson's classical work. Following this procedure and with new methods, numerous solutions for yield functions are provided by various researchers over the years. In the present work, similar attempts are made to formulate a simple closed form yield function for matrix materials dependent on strain rate. Following the same procedure as Gurson, a yield function for power law materials with spherical inclusion is studied. For the initial studies, radial symmetry of the sphere is utilized, so as to reduce the difficulty of the problem.

For the strain rate dependent matrix, the solution for a spherical inclusion with radial symmetry is given by equation.

$$\sum_{nn} = \left(\frac{2}{3}\right)^{m/2} \frac{2\sigma_0 \dot{E}_{nn}^m (1 - f^m)}{mf^m} \quad (1)$$

Similarly for the axisymmetric problem, we get :

$$\sum'_{ij} = \frac{\sigma_0}{3} \int_1^{1/f} Q^{(m-1)/2} t_{ij} X^{-2} dX \quad (2)$$

$$\sum_{nn} = \frac{\sigma_0}{3} \int_1^{1/f} 2DQ^{(m-1)/2} dX \quad (3)$$

The closed form solution can be obtained by solving the above two equations, at present various approximation methods are tested and we haven't been successful in obtaining closed form solution. The methods used for approximation are Taylor method and Gauss-Legendre. But the equation obtained can be solved numerically. A simple MATLAB program has been used to solve the equations and comparisons are made with available models and Finite element cell calculation.